

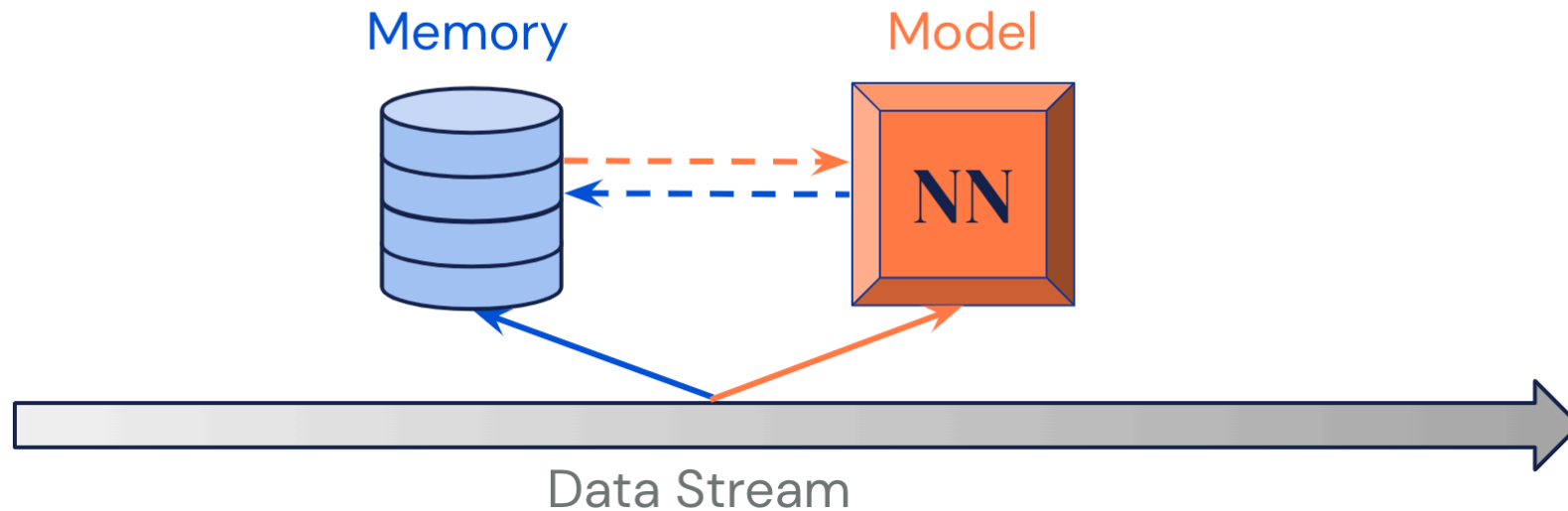
# Information-theoretic Online Memory Selection for Continual Learning

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# Online Memory Selection

- Selecting a representative memory is critical to replay-based continual learning methods.
- The agent updates both the **memory** and the **model** based on **the instant observation**,

$$(f_{\theta}, \mathcal{M}) \leftarrow (f_{\theta}, \mathcal{M}, (\mathbf{x}_{\star}, y_{\star}))$$



# Online Memory Selection

- Challenges

- The purely online constraint calls for both **effectiveness** and **efficiency**.



- To select a representative memory needs to deal with **data imbalance**.

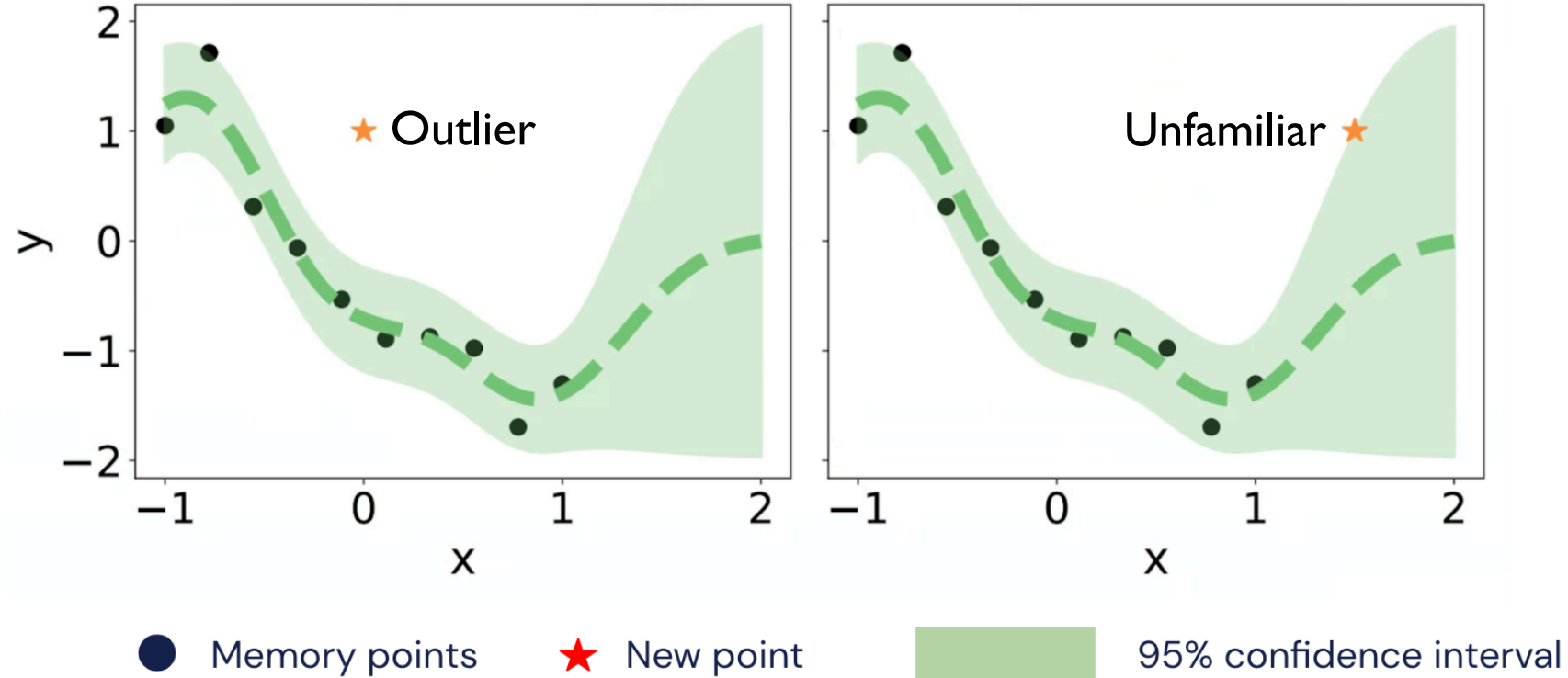


- $\mathcal{M}$  should contain **the most information** about the underlying function.

# Memorable Information Criterion

- **Surprise**: find “surprising” data points

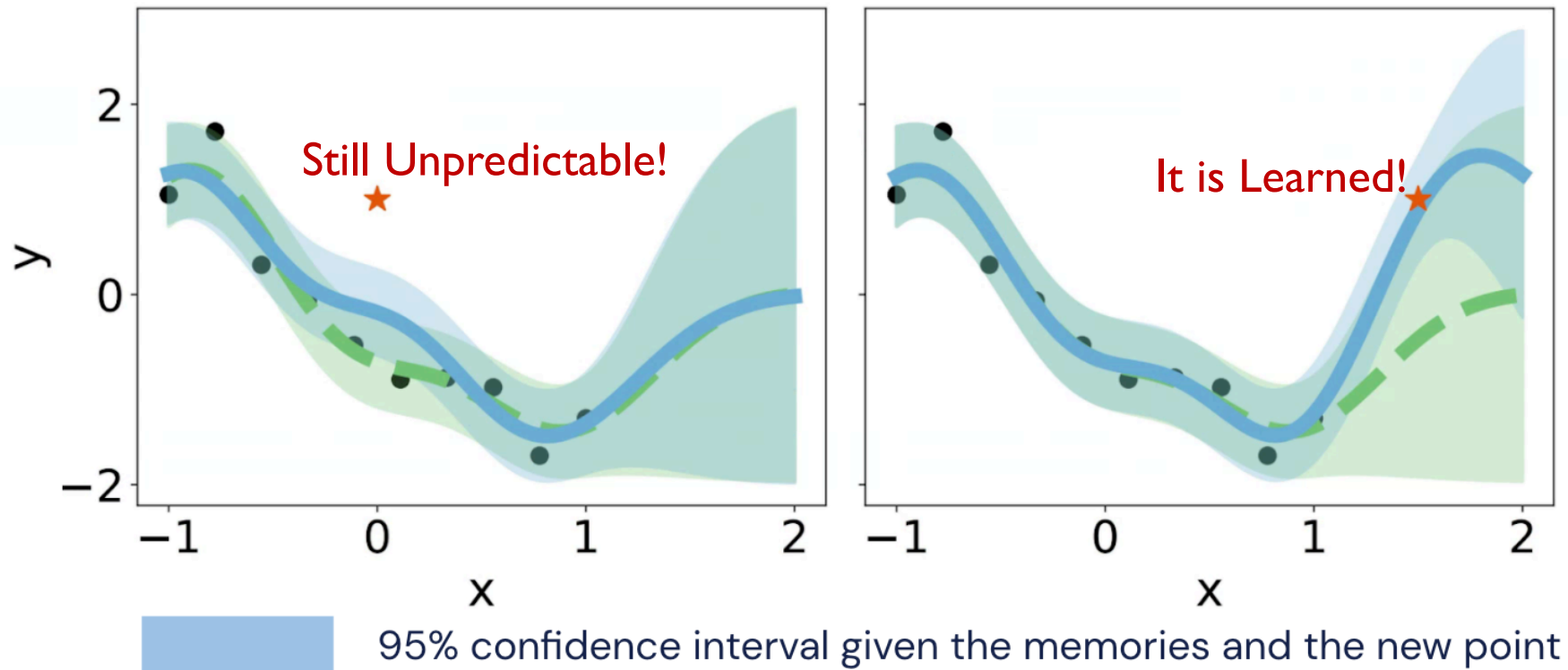
$$s_{surp}((x_*, y_*); \mathcal{M}) = -\log p(y_* | y_{\mathcal{M}})$$



# Memorable Information Criterion

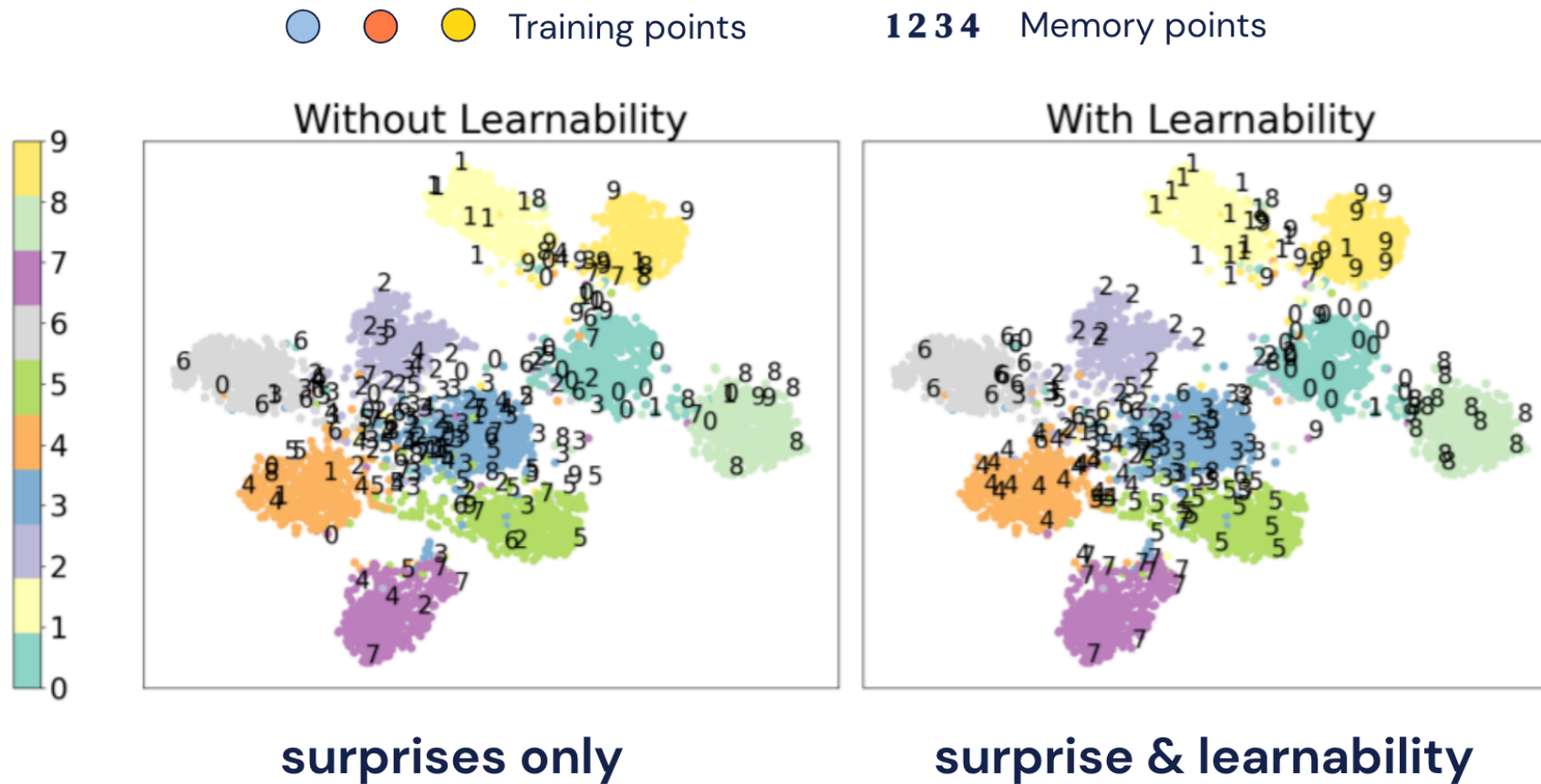
- **Learnability**: avoid “harmful” outliers

$$s_{\text{learn}}((x_*, y_*); \mathcal{M}) = \log p(y_* | y_*, y_{\mathcal{M}})$$



# Memorable Information Criterion

- **Surprise** finds unfamiliar points.
- **Learnability** avoids outliers.



# Information-theoretic Reservoir Sampling

- InfoRS: a modification of Reservoir Sampling (Vitter, 1985) to select informative points only.

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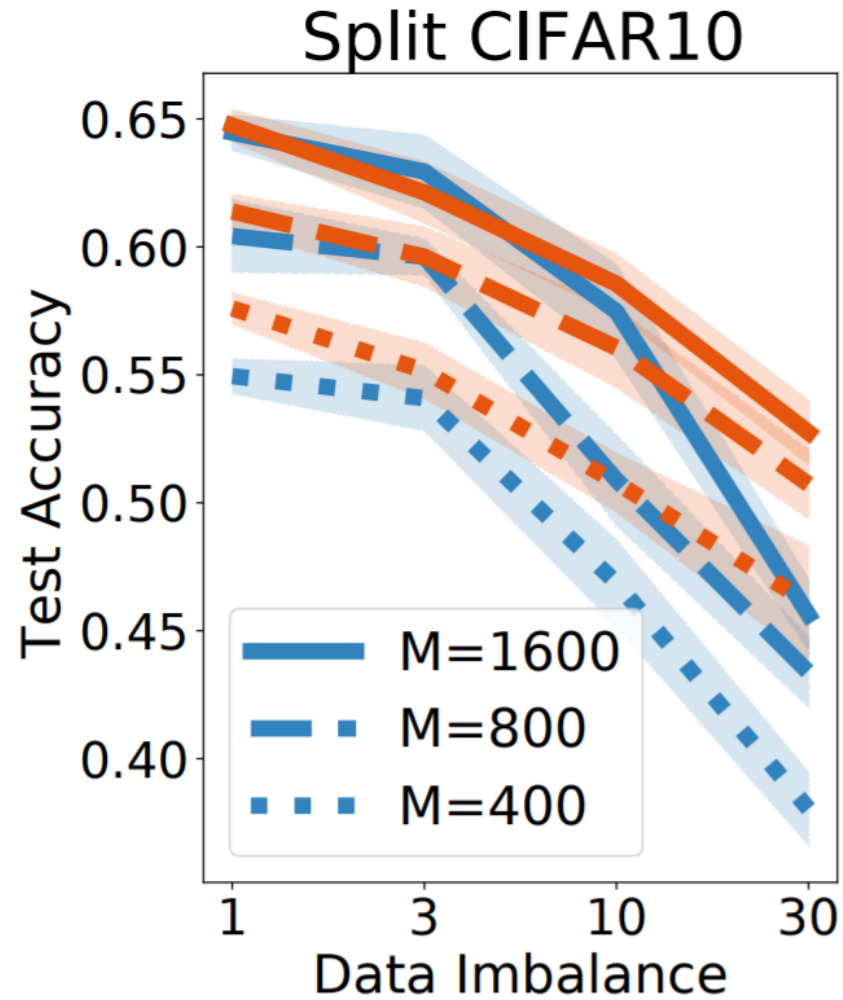
**Algorithm 1** Information-theoretic Reservoir Sampling (InfoRS)

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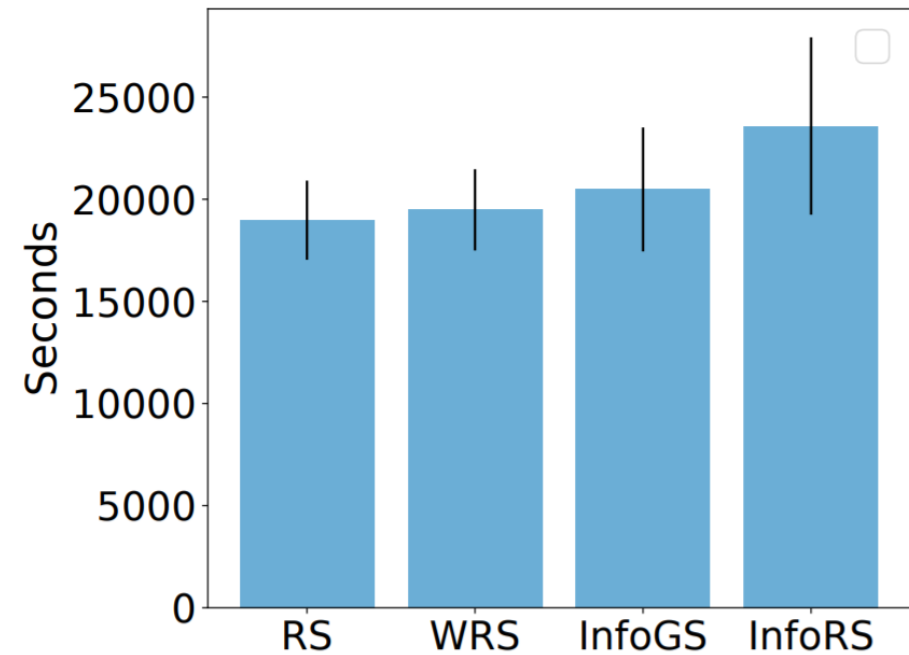
- 1: **Input:** Memory  $\mathcal{M}$  and matrices  $\mathbf{A}_{\mathcal{M}}^{-1}$ ,  $\mathbf{b}_{\mathcal{M}}$ , the batch  $\mathcal{B}$ , the predictor parameter  $\theta$ .
  - 2: **Input:** The reservoir count  $n$  and the budget  $M$ .
  - 3: **Input:** Running mean and stddev for the MIC:  $\hat{\mu}_i, \hat{\sigma}_i$ . The thresholding ratio  $\gamma_i$ .
  - 4: Update the predictor parameter  $\theta$  based on  $\mathcal{M}$  and  $\mathcal{B}$ . // Predictor Update
  - 5: Update the features for the memory points used in replay, and update  $\mathbf{A}_{\mathcal{M}}^{-1}$ ,  $\mathbf{b}_{\mathcal{M}}$  accordingly.
  - 6: **for**  $(\mathbf{x}_*, y_*)$  in  $\mathcal{B}$  **do**
  - 7:   **if**  $|\mathcal{M}| < M$  **or**  $\text{MIC}_{\eta}((\mathbf{x}_*, y_*); \mathcal{M}) \geq \hat{\mu}_i + \hat{\sigma}_i * \gamma_i$  // Information Thresholding
  - 8:     Update  $\mathcal{M}, n \leftarrow \text{ReservoirSampling}(\mathcal{M}, M, n, (\mathbf{x}_*, y_*))$ . // Memory Update
  - 9:     Update  $\mathbf{A}_{\mathcal{M}}^{-1}, \mathbf{b}_{\mathcal{M}}$  based on the Sherman-Morrison formula if  $\mathcal{M}$  is updated.
  - 10:    Update  $\hat{\mu}_i, \hat{\sigma}_i$  using the criterion  $\text{MIC}_{\eta}((\mathbf{x}_*, y_*); \mathcal{M})$ . // Running Moments Update
  - 11: **return** Buffer  $\mathcal{M}$  and  $\mathbf{A}_{\mathcal{M}}^{-1}, \mathbf{b}_{\mathcal{M}}$ . The reservoir count  $n$  and statistics  $\hat{\mu}_i, \hat{\sigma}_i$ . The updated  $\theta$ .
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# Continual Learning Experiments

Improved robustness against data imbalance



Minimal Computational Overhead





# Thanks!

*Improved robustness against data imbalance in online memory selection*